

Corollary (T. Yamamoto - 5)

$f: M^n \rightarrow N^{n-1}$ proper,

Thom-Boardman generic

f is an oriented map

(i.e. fibers of $f|_{M^n - S(f)}$ are consistently oriented)

$$\Rightarrow 3 [\mathbb{I}^{\theta}(f)]^* = f_! P_1(M)$$

in $H^3(N; \mathbb{Z})$ mod. torsion

In the following, for $I = (i_1, \dots, i_n)$,

$$W_I = W_1^{i_1} \cup \dots \cup W_n^{i_n},$$

$$P_I = P_1^{i_1} \cup \dots \cup P_n^{i_n}.$$