

↓

Univ. cpx of chiral sing. fibers  
defined over  $\mathbb{Z}$

$f : M \rightarrow N$  oriented map

DEF  
⇔

fibers of  $f|_{M-S(f)} : M-S(f) \rightarrow N$   
are consistently oriented

↑  
sing. pt set of  $f$

↓

$$\mathcal{G}_f : H^k(\text{Univ. cpx}) \rightarrow H^k(N; \mathbb{Z})$$

Sensitive to orientation of  
the source manifold.

Oriented  $\tau$ -cob. invariance holds.